

3. Use the Intermediate Value Theorem to show that $f(x) = x^3 - 2x - 1$ has a root on $[1, 2]$.
4. Use Newton's Method with an initial guess of $x_0 = 1.5$ to find the next three approximations to a solution of $x^3 - 2x - 1 = 0$. Then test your final approximation to see if it appears to be close to a root.
5. What (if anything) does the Extreme Value Theorem say about $f(x) = x^2$ on each of the following intervals?
- (a) $[1, 4]$
- (b) $(1, 4)$
6. Find the value of the constant c that the Mean Value Theorem specifies for $f(x) = x^3 + x$ on $[0, 3]$.
7. Find the following.
- (a) all antiderivatives of $1 + 2x + x^3 + 4\sqrt{x} + \frac{1}{x^5}$
- (b) $\int_1^7 \frac{3}{x} dx$
- (c) $\int_{-2}^2 \sqrt{4 - x^2} dx$
- (d) $\frac{d}{dx} \int_1^x \sin \sqrt{t} dt$

$$(e) \lim_{n \rightarrow \infty} \frac{2}{n} \sum_{k=1}^n \left(1 + \frac{2k}{n}\right)^2$$

[The 8:00 and 9:30 sections may omit this part.]

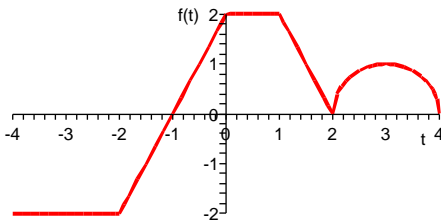
8. Water is leaking out of a tank at a decreasing rate $r(t)$ as shown in the table below.

time (min)	0	2	4	6	8
rate (gal/min)	15	11	8	4	3

(a) Find an overestimate and underestimate for the total amount that leaked out during these 8 minutes.

(b) Interpret the expression $\int_2^6 r(t) dt$ in terms of the situation described above.

9. Consider the graph of $f(t)$ shown. It is made of straight lines and a semicircle.



$$\text{Let } G(x) = \int_0^x f(t) dt \text{ and } H(x) = \int_{-3}^x f(t) dt.$$

(a) Compute $G(2)$, $G(4)$, and $H(4)$.

(b) Where is G increasing? Where is G decreasing?

(c) Where is G concave up? Where is G concave down?

(d) At what x -value(s) does G have a local maximum? At what x -value(s) does G have a local minimum?

(e) Find a formula that relates G and H .

(f) How would your answers to (b), (c), and (d) change if the questions were about H instead of G ?

10. (a) Use sigma notation to express L_{10} and M_{10} as approximations to $\int_{20}^{60} \ln x \, dx$.

(b) Draw a sketch that represents the sum M_4 .

11. Your company is mass-producing a cylindrical container. The flat portion (top and bottom) costs 3 cents per square inch and the curved (lateral) portion costs 5 cents per square inch. If your budget is \$9.00 per container, what dimensions will give the largest volume? [The 8:00 and 9:30 sections may omit this problem.]

$$\text{area of circle} = \pi r^2$$

$$\text{lateral area of cylinder} = 2\pi r h$$

$$\text{volume of cylinder} = \pi r^2 h$$