Lesson One: The Basics

Font Families
I love math!
\LaTeX does not rhyme with “paychecks”!

Math Environments, Superscripts, and Subscripts
The numbers 3, 4, and 5 are a Pythagorean triple because \(3^2 + 4^2 = 5^2\).

We all know that \((x^n)' = nx^{n-1}\), but what is \((x^x)'\)?

The recursive definition for the Fibonacci numbers is \(F_1 = 1, F_2 = 1, \text{ and } F_n = F_{n-1} + F_{n-2}\) for all integers \(n > 2\).

Compare \(\frac{1}{a+b} \neq \frac{1}{a} + \frac{1}{b}\) to the following.

\[
\frac{1}{a + b} \neq \frac{1}{a} + \frac{1}{b}
\]

We can also display it midline by using “display-style”: \(\frac{1}{a + b} \neq \frac{1}{a} + \frac{1}{b}\).

Exercise One: The Basics
A certain math professor will scream and may even cry if you confuse the Latin terms \(id est\), meaning “that is to say” and \(exempli gratia\), meaning “for instance.”

Compare the following.

I adore polynomials, \(e.g., x^4 + x^2 + 1\).
I adore polynomials, \(i.e.,\) expressions of the form \(a_0 + a_1 x + a_2 x^2 + \cdots + a_n x^n\), where \(a_0, a_1, \ldots, a_n\) are constants and \(n\) is a non-negative integer.

Do you lie awake at night wondering what is the smallest positive integer that can be written as the sum of two perfect cubes in two distinct ways? Well, wonder no more:

\[1729 = 10^3 + 9^3 = 12^3 + 1^3\]

We all learned in first grade that \((a + b)^3 \neq a^3 + b^3\), but when we study modular arithmetic we’ll find that the two are equal in “mod 3.”

The famous mathematician Euler (rhymes with “boiler” \textbf{NOT} with “ruler”) used the geometric series formula \(a + ar + ar^2 + ar^3 + \cdots = a/(1 - r)\) to conclude the following.

\[1 - 1 + 1 - 1 + 1 - \cdots = \frac{1}{2}\]

But we know the formula only applies if \(-1 < r < 1\), so this result is not valid.