Suppose $S$ is the solid unit sphere, i.e. the solid ball centered at the origin with radius 1 unit.

By changing variables to spherical coordinates, set up but do not evaluate the integral that gives the value of:

$$\iiint_S (x + y) \, dx \, dy \, dz$$